

**DO NOW**

The vertices of quadrilateral  $PQRS$  are  $P(1,1)$ ,  $Q(4,-2)$ ,  $R(7,1)$ , and  $S(4,4)$ . Is  $PQ$  parallel to  $RS$ ? Show your work and explain your answer.

$$\text{Slope } PQ = \frac{-2-1}{4-1} = \frac{-3}{3} = -1$$

$$\text{Slope } RS = \frac{4-1}{4-7} = \frac{3}{-3} = -1$$

$\overline{PQ} \parallel \overline{RS}$  because their slopes are equal

Jan 24-9:52 AM

Proving a Quadrilateral is a Trapezoid

At least one pair of sides **MUST BE PARALLEL**

Show this using the slope formula

Given:  $A(1,6)$ ,  $B(7,9)$ ,  $C(10,6)$ , and  $D(0,1)$

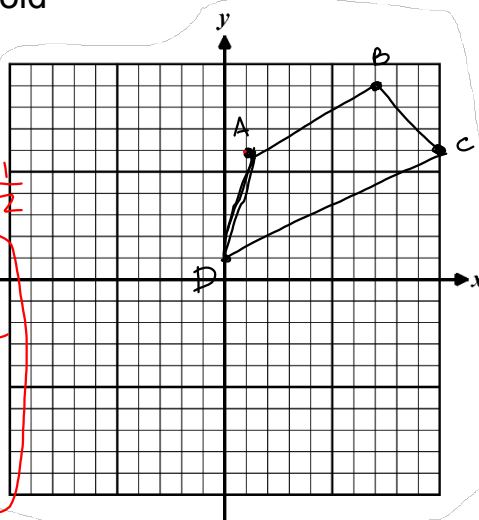
Prove:  $ABCD$  is a trapezoid

$$\text{Slope } AB = \frac{9-6}{7-1} = \frac{3}{6} = \frac{1}{2}$$

$$\text{Slope } DC = \frac{6-1}{10-0} = \frac{5}{10} = \frac{1}{2}$$

$\overline{AB}$  and  $\overline{DC}$  have the same slope so  $\overline{AB} \parallel \overline{DC}$

$ABCD$  is a trapezoid b/c it has one pair of parallel sides



Jan 3-10:00 AM

## Proving a Quadrilateral is a Parallelogram

Two pairs of opposite sides parallel

Using slope formula (4x)

OR

Two pairs of opposite sides congruent

Using distance formula (4x)

OR

The diagonals bisect each other

Using midpoint formula (2x)

Dec 14-7:47 AM

The vertices of quadrilateral  $ABCD$  are  $A(-2,1)$ ,  $B(4,-2)$ ,  $C(8,2)$  and  $D(2,5)$ .  
Prove  $ABCD$  is a parallelogram.

(a) Using slopes      (b) Using distance      (c) Using midpoints

(a)

$$\text{Slope } AB = \frac{-2-1}{4-(-2)} = \frac{-3}{6} = -\frac{1}{2}$$

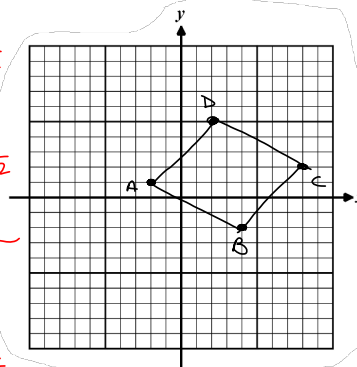
$$\text{Slope } BC = \frac{2-(-2)}{8-4} = \frac{4}{4} = 1$$

$$\text{Slope } CD = \frac{5-2}{2-8} = \frac{3}{-6} = -\frac{1}{2}$$

$$\text{Slope } AD = \frac{5-1}{2-(-2)} = \frac{4}{4} = 1$$

slope of  $AB = \text{slope } CD$   
and slope  $BC = \text{slope } AD$ ,  
 $\overline{AB} \parallel \overline{CD}$  and  $\overline{BC} \parallel \overline{AD}$

A quad w/ two pairs of  
opp. sides  $\parallel$  is a parallelogram



Dec 14-7:52 AM

The vertices of quadrilateral  $ABCD$  are  $A(-2,1)$ ,  $B(4,-2)$ ,  $C(8,2)$  and  $D(2,5)$ . Prove  $ABCD$  is a parallelogram.

(a) Using slopes      (b) Using distance      (c) Using midpoints

(b)

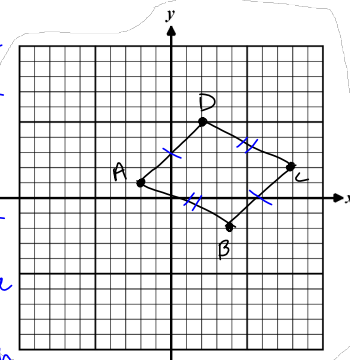
$$AB = \sqrt{(-2-4)^2 + (1-(-2))^2} = \sqrt{45}$$

$$BC = \sqrt{(4-8)^2 + (-2-2)^2} = \sqrt{32}$$

$$CD = \sqrt{(8-2)^2 + (2-5)^2} = \sqrt{45}$$

$$AD = \sqrt{(-2-2)^2 + (1-5)^2} = \sqrt{32}$$

$\overline{AB} \cong \overline{CD}$  and  $\overline{BC} \cong \overline{AD}$   
 because they are the same length.  $ABCD$  is a parallelogram b/c both pairs of opp sides are  $\cong$



Dec 14-7:52 AM

The vertices of quadrilateral  $ABCD$  are  $A(-2,1)$ ,  $B(4,-2)$ ,  $C(8,2)$  and  $D(2,5)$ . Prove  $ABCD$  is a parallelogram.

(a) Using slopes      (b) Using distance      (c) Using midpoints

(c)

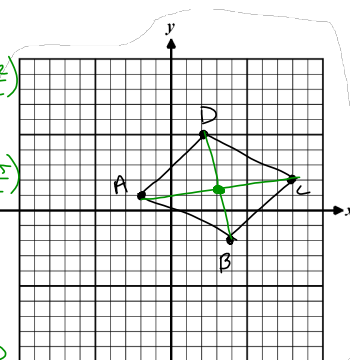
$$\text{Midpoint } AC = \left( \frac{-2+8}{2}, \frac{1+2}{2} \right)$$

$$\left( 3, \frac{3}{2} \right)$$

$$\text{Midpoint } BD = \left( \frac{4+2}{2}, \frac{-2+5}{2} \right)$$

$$\left( 3, \frac{3}{2} \right)$$

$\overline{AC}$  and  $\overline{BD}$  have the same midpoint so they bisect each other.  $ABCD$  is a parallelogram b/c its diagonals bisect each other



Dec 14-7:52 AM

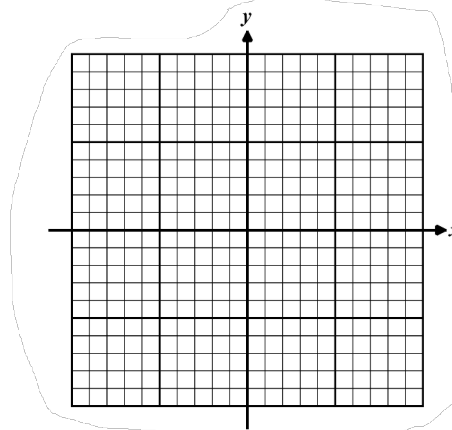
Quadrilateral  $RSTU$  has vertices at  $R(-4,4)$ ,  $S(2,7)$ ,  $T(5,2)$  and  $U(-7,-4)$ . Show that  $RSTU$  is a trapezoid but *not* a parallelogram. Use of the grid is optional.

$$\text{slope } RS =$$

$$\text{slope } ST =$$

$$\text{slope } TU =$$

$$\text{slope } RU =$$



Jan 24-9:52 AM