

**DO NOW**

Rhombus  $STAR$  has vertices  $S(-1,2)$ ,  $T(2,3)$ ,  $A(3,0)$ , and  $R(0,-1)$ . What is the perimeter of rhombus  $STAR$ ?

- 1)  $\sqrt{34}$
- 2)  $4\sqrt{34}$
- 3)  $\sqrt{10}$
- 4)  $4\sqrt{10}$

$$ST = \sqrt{(-1-2)^2 + (2-3)^2}$$

$$ST = \sqrt{10}$$

$$4\sqrt{10}$$

### Area of Polygons in the Coordinate Plane

"Box Out" the shape, creating a rectangle and right  $\Delta$ 's

Find the area of the rectangle and each right  $\Delta$

Subtract:

Area of Rect - Area of Right  $\Delta$ 's

1) Triangle  $RST$  is graphed on the set of axes below.

$$A_{\text{rect}} = 12 \cdot 12$$

$$A = 144$$

$$A_{\Delta I} = \frac{1}{2}(3 \cdot 6)$$

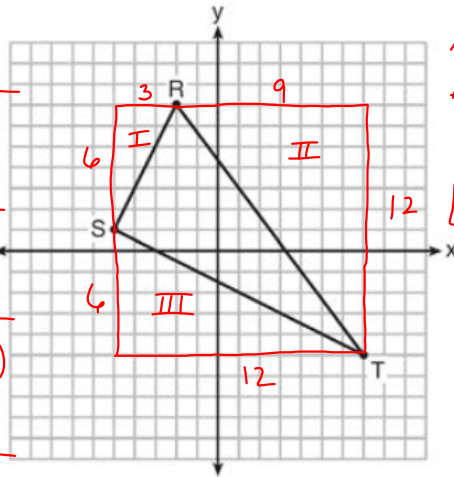
$$\Delta I = 9$$

$$A_{\Delta II} = \frac{1}{2}(9 \cdot 12)$$

$$\Delta II = 54$$

$$A_{\Delta III} = \frac{1}{2}(6 \cdot 12)$$

$$\Delta III = 36$$



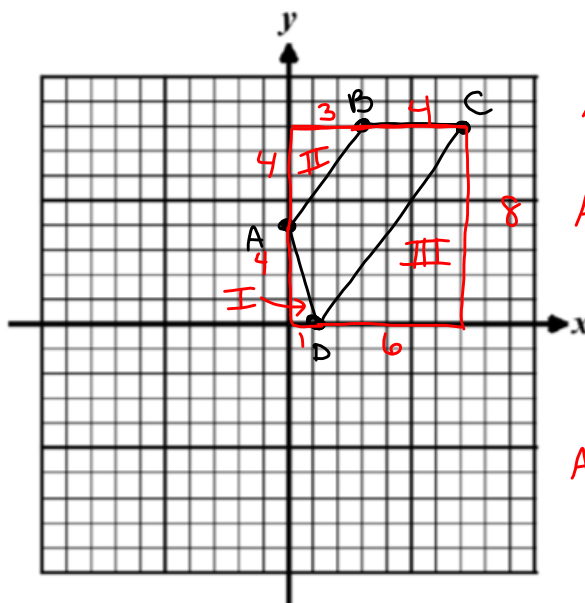
Area of  $\Delta RST = 144 - 99$

$\Delta RST = 45$

How many square units are in the area of  $\Delta RST$ ?

- 1)  $9\sqrt{3} + 15$
- 2)  $9\sqrt{5} + 15$
- 3) 45
- 4) 90

2) Find the area of trapezoid  $ABCD$  with vertices  $A(0,4)$ ,  $B(3,8)$ ,  $C(7,8)$  and  $D(1,0)$



$$A_{\text{rect}} = 7 \cdot 8 = 56$$

$$A_{\Delta I} = \frac{1}{2}(1 \cdot 4) = 2$$

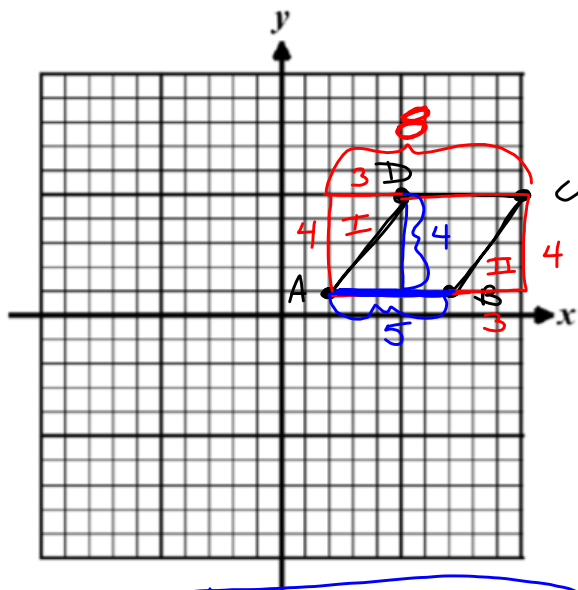
$$A_{\Delta II} = \frac{1}{2}(3 \cdot 4) = 6$$

$$A_{\Delta III} = \frac{1}{2}(6 \cdot 8) = 24$$

Area of  $ABCD = 56 - 32$

$= 24$

- 3) Find the area of parallelogram  $ABCD$  with vertices  $A(2, 1)$ ,  $B(7, 1)$  and  $C(10, 5)$  and  $D(5, 5)$



$$A_{\text{rect}} = 8 \cdot 4 = 32$$

$$A_{\Delta I} = \frac{1}{2}(3 \cdot 4) = 6$$

$$A_{\Delta II} = \frac{1}{2}(3 \cdot 4) = 6$$

$$32 - 12$$

$$\boxed{20}$$

$$A = 5 \cdot 4 = 20$$

- 4) On the set of axes below, the vertices of  $\triangle PQR$  have coordinates  $P(-6, 7)$ ,  $Q(2, 1)$ , and  $R(-1, -3)$ .

- (a) What is the area of  $\triangle PQR$ ?

$$A_{\text{rect}} = 8 \cdot 10 = 80$$

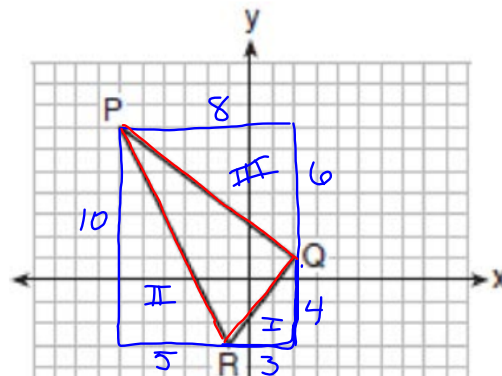
$$A_{\Delta I} = \frac{1}{2}(3 \cdot 4) = 6$$

$$A_{\Delta II} = \frac{1}{2}(5 \cdot 10) = 25$$

$$A_{\Delta III} = \frac{1}{2}(6 \cdot 8) = 24$$

$$\text{Area of } \triangle PQR = 80 - 55$$

$$= \boxed{25}$$



- (b) What is the perimeter of  $\triangle PQR$ ?

$$PR^2 = 5^2 + 10^2$$

$$PR = \sqrt{125}$$

$$\sqrt{25} \cdot \sqrt{5}$$

$$5\sqrt{5}$$

$$RQ^2 = 3^2 + 4^2$$

$$RQ = 5$$

$$PQ^2 = 6^2 + 8^2$$

$$PQ = 10$$

$$P \text{ of } \triangle PQR = 15 + 5\sqrt{5}$$