

### Law of Cosines

$$c^2 = a^2 + b^2 - 2ab \cos C$$

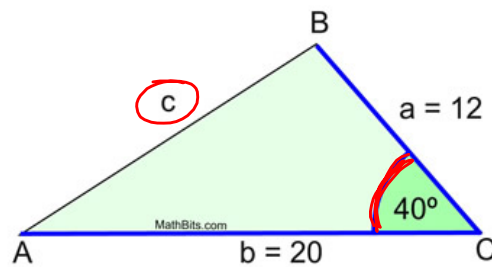
$$b^2 = a^2 + c^2 - 2ac \cos B$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$



In  $\triangle ABC$ ,  $m\angle C = 40^\circ$ ,  $a = 12$ , and  $b = 20$ .

Find side  $c$  to the *nearest integer*.



$$c^2 = (12)^2 + (20)^2 - 2(12)(20) \cdot \cos 40$$

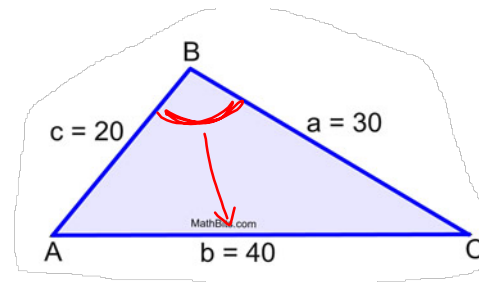
$$\sqrt{c^2} = \sqrt{176.2986 \dots}$$

$$c = 13.2777 \dots$$

$$\boxed{13}$$

In  $\triangle ABC$ ,  $a = 30$ ,  $b = 40$ , and  $c = 20$ .

Find the number of degrees in the largest angle  
(to the nearest degree).



$$40^2 = (20)^2 + (30)^2 - 2(20)(30) \cdot \cos B$$

$$1600 = 1300 - 1200 \cos B$$

$$\begin{array}{r} -1300 \\ \hline \end{array}$$

$$\frac{300}{-1200} = \frac{-1200(\cos B)}{-1200}$$

$$\frac{-300}{1200} = \cos B$$

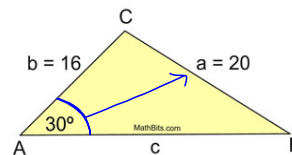
$$\rightarrow \cos^{-1}\left(\frac{-300}{1200}\right)$$

$$m\angle B = 104.4775\dots$$

$$\boxed{104^\circ}$$

In  $\triangle ABC$ ,  $m\angle A = 30^\circ$ ,  $a = 20$ , and  $b = 16$ .

Find  $c$ .



$$20^2 = (16)^2 + c^2 - 2(16)(c) \cdot \cos 30$$

$$400 = 256 + c^2 - 27.7128c$$

$$\begin{array}{r} -400 \\ \hline \end{array}$$

$$(a) \quad (b) \quad (c) \quad |c^2 - 27.7128c - 144 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{27.7128 \pm \sqrt{(-27.7128)^2 - 4(1)(-144)}}{2(1)}$$

$$x = \frac{27.7128 \pm \sqrt{1343.9992}}{2}$$

$$\frac{27.7128 + \sqrt{1343.9992}}{2}$$

$$\frac{27.7128 - \sqrt{1343.9992}}{2}$$

$$31.8942$$

$$-4.7662$$

$$\boxed{32}$$