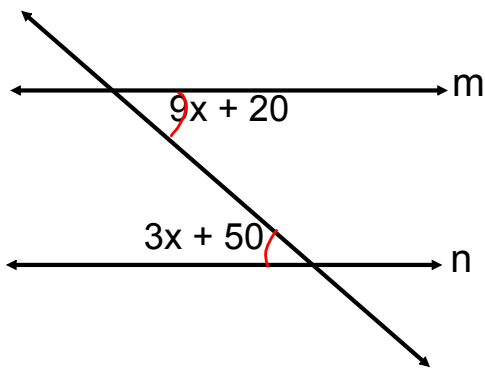


DO NOW

Line m is parallel to line n. Find the value of x



$$9x + 20 = 3x + 50$$

$$6x + 20 = 50$$

$$6x = 30$$

$$x = 5$$

Dec 10-10:13 AM

2

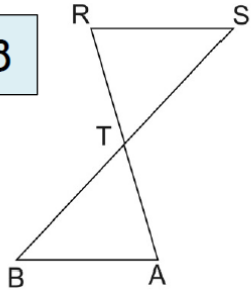
Given: \overline{RAP} ; \overline{TAD}
 \overline{RP} bis \overline{TD}
 \overline{TD} bis \overline{RP}

Prove: $\overline{TR} \parallel \overline{PD}$

Statements	Reasons
1. \overline{RAP} ; \overline{RP} bis \overline{TD} \overline{TD} bis \overline{RP}	1. Given
2. $\overline{TA} \cong \overline{DA}$; $\overline{RA} \cong \overline{PA}$	2. Bisector of a segment forms 2 \cong segments.
3. $\angle TAR \cong \angle DAP$	3. Vertical \angle s are \cong .
4. $\triangle TAR \cong \triangle DAP$	4. SAS: If 2 sides and the included \angle of 1 \triangle are \cong to the corres. parts of a 2nd \triangle , the \triangle s are \cong .
5. $\angle R \cong \angle P$ (or $\angle T \cong \angle D$)	5. CPCTC: Corres. parts of \cong \triangle s are \cong .
6. $\overline{TR} \parallel \overline{PD}$	6. If 2 lines are cut by a trans. and alt. int. \angle are \cong , the lines are parallel.

Nov 20-8:28 AM

3



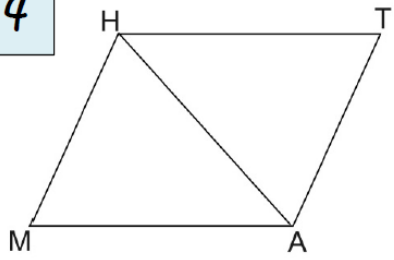
Given: $\overline{RS} \parallel \overline{BA}$; $\overline{RS} \cong \overline{BA}$
 \overline{RTA} ; \overline{STB}

Prove: \overline{RA} and \overline{SB} bisect each other

Statements	Reasons
1. $\overline{RS} \parallel \overline{BA}$; $\overline{RS} \cong \overline{BA}$ \overline{RTA} ; \overline{STB}	1. Given
2. $\angle R \cong \angle A$ $\angle S \cong \angle B$	2. If 2 \parallel lines are cut by a trans., the alt. int. \angle s are \cong .
3. $\triangle RST \cong \triangle ABT$	3. ASA: If 2 \angle s and incl. side of 1 \triangle are \cong to the corres. parts of another \triangle , the \triangle s are \cong .
4. $\overline{BT} \cong \overline{ST}$; $\overline{RT} \cong \overline{AT}$	4. CPCTC: Corres. parts of \cong \triangle s are \cong .
5. \overline{RA} bis \overline{SB} ; \overline{SB} bis \overline{RA}	5. A segment bisector divides a segment into 2 \cong segments.

Nov 20-8:28 AM

4



Given: $\overline{MH} \cong \overline{TA}$
 $\angle M \cong \angle T$
 $\angle MHA \cong \angle TAH$

Prove: $\overline{HT} \parallel \overline{MA}$

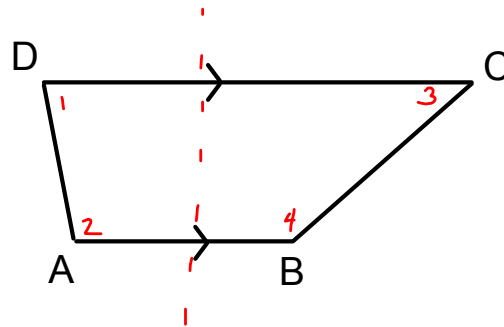
Statements	Reasons
1. $\overline{MH} \cong \overline{TA}$ $\angle M \cong \angle T$ $\angle MHA \cong \angle TAH$	1. Given
2. $\triangle MHA \cong \triangle TAH$	2. ASA: If 2 \angle s and the included side of 1 \triangle are \cong to corres. parts of another \triangle , the \triangle s are \cong .
3. $\angle MAH \cong \angle THA$	3. CPCTC: Corres. parts of \cong \triangle s are \cong .
4. $\overline{HT} \parallel \overline{MA}$	4. If 2 lines are cut by a trans. and the alt. int. \angle s are \cong , the lines are parallel.

Nov 20-8:29 AM

Trapezoid

A quadrilateral in which AT LEAST one pair of sides are parallel

$$AB \parallel CD$$

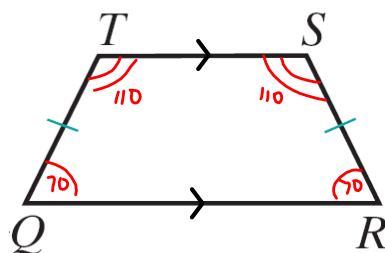


Consecutive angles are supplementary
(between the parallel lines)

Dec 21-10:25 AM

Isosceles Trapezoid

A trapezoid in which the *nonparallel* sides are CONGRUENT



$$QR \parallel TS$$

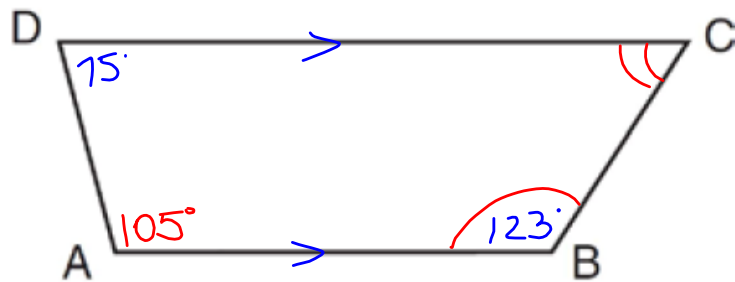
$$QT \cong SR$$

The base angles are also congruent:

$$\angle Q \cong \angle R \quad \text{and} \quad \angle T \cong \angle S$$

Dec 21-10:26 AM

In the diagram below, \overline{AB} and \overline{CD} are bases of trapezoid $ABCD$.



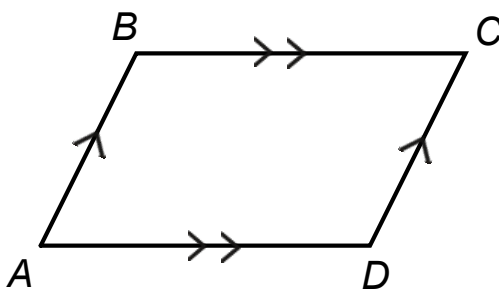
(Not drawn to scale)

If $m\angle B = 123$ and $m\angle D = 75$, what is $m\angle C$?

$$m\angle C = 57^\circ$$

Nov 20-1:19 PM

A **parallelogram** is a quadrilateral that has two pairs of opposite sides parallel

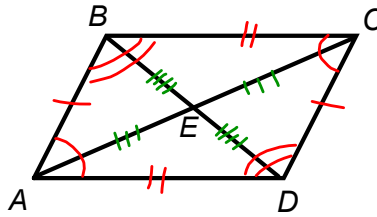


$$\begin{aligned} AB &\parallel CD \\ BC &\parallel AD \end{aligned}$$

A parallelogram is a TRAPEZOID

Dec 10-10:15 AM

Properties of Parallelograms



- Opposite **SIDES** are congruent
 $\overline{AB} \cong \overline{CD}$ and $\overline{BC} \cong \overline{AD}$
- Opposite **ANGLES** are congruent
 $\angle A \cong \angle C$ and $\angle B \cong \angle D$

Trapezoids

- Two consecutive angles are supplementary
 EX: $\angle A + \angle B = 180$
- The diagonals bisect each other
 $\overline{AE} \cong \overline{EC}$ and $\overline{BE} \cong \overline{DE}$

Dec 10-10:20 AM

The diagonals of parallelogram $ABCD$ intersect at E . If $AE = 5x - 3$ and $EC = 15 - x$, find AC .

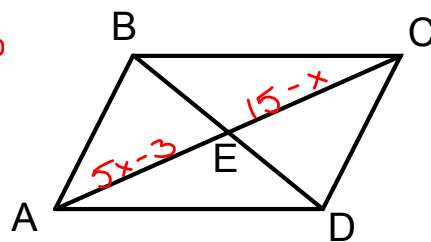
$$AE = 5(3) - 3$$

$$AE = 12$$

$$EC = 15 - 3$$

$$EC = 12$$

$$AC = 24$$



$$\overline{AE} \cong \overline{CE}$$

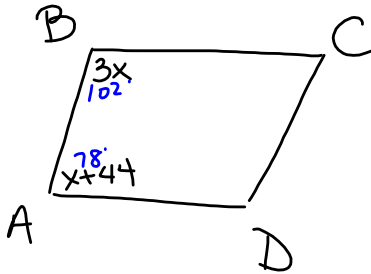
$$5x - 3 = 15 - x$$

$$6x = 18$$

$$x = 3$$

Dec 10-10:57 AM

In parallelogram $ABCD$, $m\angle A = x + 44$ and $m\angle B = 3x$. Find the measure of each angle of the parallelogram.



$$3x + x + 44 = 180$$

$$4x + 44 = 180$$

$$4x = 136$$

$$x = 34$$

$$m\angle A = 78^\circ$$

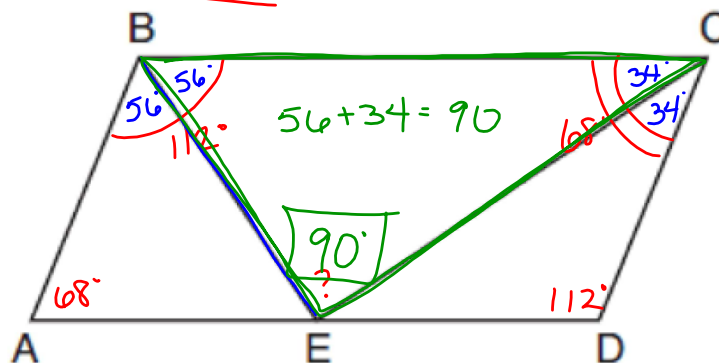
$$m\angle B = 102^\circ$$

$$m\angle C = 78^\circ$$

$$m\angle D = 102^\circ$$

Dec 10-10:42 AM

In parallelogram $ABCD$ shown below, the bisectors of $\angle ABC$ and $\angle DCB$ meet at E , a point on \overline{AD} .



If $m\angle A = 68^\circ$, determine and state $m\angle BEC$.

Nov 20-1:16 PM